

Basic Syntax

<code>null []</code>	return <i>True</i> if list is empty
<code>'H' `elem` "Hello"</code>	return <i>True</i> if H is in the string
<code>head [1,2,3]</code>	return 1
<code>tail [1,2,3]</code>	return [2,3]
<code>last [1,2,3]</code>	return 3
<code>init [1,2,3]</code>	return [1,2]
<code>:t</code>	return the type
<code>fst (5,2)</code>	return 5
<code>snd (5,2)</code>	return 2
<code>1:2:3:[]</code>	same as [1,2,3]
<code>length []</code>	give length of list
<code>reverse []</code>	reverse the list
<code>[] !! n</code>	gives the <i>nth</i> element
<code>filter test []</code>	return everything that passes the test
<code>[] ++ []</code>	list concatenation
<code>[] : []</code>	list concatenation
<code>drop n []</code>	delete the first <i>n</i> element from list
<code>take n []</code>	make a new list containing just the first <i>N</i> element
<code>splitAt n []</code>	split list into two lists at <i>nth</i> position
<code>zip [a..] [0..]</code>	combine two list into tuples [(a,0)..]
<code>map function []</code>	apply a function to all list elements

Terminology

Terminology (cont)

Type	Lower case, can be of any
Variable	type. e.g. <code>fst::(a,b)->a</code>
Typeclass	A sort of interface that defines some behavior. Basic type classes: Read, Show, Ord, Eq, Enum, Num. Num includes <i>Int</i> , <i>Integer</i> , <i>Float</i> , <i>Double</i> .
Higher-ordered Functions	A function that takes other functions as arguments or returns a function as result. Ex: <code>foldl</code> , <code>foldr</code> , <code>zipWith</code> , <code>flip</code> .
Module	A collection of related functions, types and typeclasses
Referential Transparency	An expression is called referentially transparent if it can be replaced with its corresponding value without changing the program's behavior.

substituting equals for equals, different from other programming languages

Type Signatures

In type signature, specific (*String*) and general (*a,b*) types can be mixed and matched.

<code>concat 3:: String -> String -> String</code>	Functional Use recursion instead of iteration
<code>const :: a -> b -> a</code>	Allows operations on functions
<code>allEqual :: (Eq a) => a -> a -> a -> Bool</code>	Lazy Don't do an operation unless you need the result.
<code>(.) :: (b -> c) -> (a -> b) -> a -> c</code>	

Type Signatures (cont)

Lambda function, lead with `\`, then arguments, then `->`, then the computation

Data Types

Haskell uses various data types, all of them starts by a capital letter:

- Int**: Integer number with fixed precision
- Integer**: Integer number with virtually no limits
- Float**: Floating number
- Bool**: Boolean. Takes two values: True or False.
- Char**: Character. Any character in the code is placed between quotes (').
- String**: Strings (In fact, a list of Chars).

Properties of Haskell

Pure	No side effects in functions and expressions
	No assignment operators such as <code>++</code> and <code>=+</code>
	<i>I/O is an exception</i>
	Promotes referential transparency
	Once <i>x</i> is assigned to a value, the value stays the same
	Functional Use recursion instead of iteration
	Allows operations on functions
	Lazy Don't do an operation unless you need the result.
	<code>(\x->1.0+x)^5</code>

Recursive Descent Parser

```
-- our parsers generally are of
type Parser [Ptree]
data Ptree = VAR String | ID
String | FCN String [Ptree]
deriving (Show, Eq, Read)
data Presult a = FAIL | OK a
String deriving (Show, Eq, Read)
type Parser a = String ->
Presult a
```

Polymorphic Types Families of types. For example, $(\text{forall } a)[a]$ is the family of types consisting of, for every type a , the type of lists of a . Lists of integers (e.g. $[1,2,3]$), lists of characters ($['a','b','c']$), even lists of lists of integers, etc., are all members of this family.



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Recursive Descent Parser (cont)

```
> -- As before, we use &> and |> as AND /
OR combinators on parsers
expr = variable |> fcnCall |> identifier
fcnCall = buildCall . (identifier &> skip "(" &>
arguments &> skip ")")
arguments = expr &> argTail |> empty
argTail = skip "," &> expr &> argTail |>
empty
identifier input = beginsWith ID Data.C-
har.isLower isTailChar (dropblank input)
variable input = beginsWith VAR Data.C-
har.isUpper isTailChar (dropblank input)
empty = OK [] -- empty string parser always
succeeds
```

UTILITY ROUTINES

```
-- Parse a string but don't save it as a parse
tree
```

```
skip :: String -> Parser [a]
```

```
skip want input =
```

```
    let found = take (length want) input
        remainder = dropblank (drop (length
want) input)
```

```
    in
```

```
        if want == found then OK [] remainder
        else FAIL
```

```
-- Build a singleton list of a function call
```

```
parse tree from a list with
```

```
-- an identifier followed by list of arguments
```

```
buildCall :: Presult [Ptree] -> Presult [Ptree]
```

```
buildCall FAIL = FAIL
```

```
buildCall (OK []) = FAIL
```

```
buildCall (OK (ID fcn : args) remainder) =
```

```
OK [FCN fcn args] remainder
```

```
-- Build a singleton list of a parse tree given
```

```
the kind of tree we want
```

```
-- and the kinds of head and tail characters
```

```
we want
```

```
beginsWith :: (String -> Ptree) -> (Char ->
```

```
Bool) -> (Char -> Bool) -> Parser [Ptree]
```

Recursive Descent Parser (cont)

```
> beginsWith _ _ _ "" = FAIL
```

```
beginsWith builder isHead isTail (c:cs)
```

```
    | isHead c = let tail = Data.List.takeWhile
```

```
isTail cs
```

```
        in OK [builder (c:tail)] (dropblank
```

```
(drop (length tail) cs))
```

```
    | otherwise = FAIL
```

```
-- Remove spaces (and tabs and newlines)
```

```
from head of string.
```

```
--
```

```
dropblank :: String -> String
```

```
dropblank = Data.List.dropWhile Data.C-
```

```
har.isSpace
```

```
-- kind of character that makes up 2nd - end
```

```
character of an id or var
```

```
--
```

```
isTailChar :: Char -> Bool
```

```
isTailChar c = Data.Char.isAlphaNum c || c
```

```
== '_'
```

```
-----
```

```
-- Concatenation and alternation operators
```

```
on parsers
```

```
-- (|>) is an OR/Alternation operator for
```

```
parsers.
```

```
--
```

```
infixr 2 |>
```

```
(|>) :: Parser a -> Parser a -> Parser a
```

```
(p1 |> p2) input =
```

```
    case p1 input of
```

```
        m1 @ (OK _) -> m1 -- if p1
```

```
succeeds, just return what it did
```

```
        FAIL -> p2 input
```

```
-- (&>) is an AND/Concatenation operator
```

```
for parsers
```

```
infixr 3 &>
```

```
(&>) :: Parser [a] -> Parser [a] -> Parser [a]
```

```
(p1 &> p2) input =
```

```
    case p1 input of
```

```
        FAIL -> FAIL -- p1 fails? we fail
```

```
        OK ptrees1 remain1 ->
```

Recursive Descent Parser (cont)

```
> case p2 remain1 of -- run p2 on
```

```
remaining input
```

```
    FAIL -> FAIL -- p2 fails? we fail
```

```
    OK ptrees2 remain2 -> -- both
```

```
succeeded
```

```
        OK (ptrees1 ++ ptrees2)
```

```
remain2
```

Tree

```
data Tree a = Leaf a | Branch a (T
```

```
treeEq :: (Eq a) => Tree a -> Tree
```

```
treeEq (Leaf x) (Leaf y) = x == y
```

```
treeEq (Branch x1 l1 r1) (Branch x
```

```
treeEq _ _ = False
```

```
treeShow
```

```
treeShow :: Show a => Tree a -> [C
```

```
treeShow (Leaf x) = " (Leaf " ++ s
```

```
treeShow (Branch x left right) = "
```

```
"
```

Preorder via standard recursion

```
preorder :: Tree a -> [a]
```

```
preorder (Leaf x) = [x]
```

```
preorder (Branch x left right) = x
```

Tail-recursive traversal

```
preorder' :: Tree a -> [a] -> [a]
```

```
preorder' (Leaf x) xs = x : xs
```

```
preorder' (Branch r left right) xs
```

Function Syntax

```
addFour w x y z =
```

```
    let a = w + x
```

```
        b = y + a
```

```
    in z + b
```

```
-----
```

```
addFour w x y z =
```

```
    z + b
```



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Function Syntax (cont)

> where

a = w + x

b = y + a

fib n

| n < 2 = 1

| otherwise = fib (n - 1) + fib (n - 2)

fib n =

case n of

0 -> 1

1 -> 1

fib n =

if n < 2

then 1

else fib (n - 1) + fib (n - 2)

nameReturn :: IO String

nameReturn = do putStr "What is your name? "

name <- getLine

putStrLn ("Pleased to meet you, "

++ name ++ "!")

return full

Regex

. Any character except new line (\n)

\w Word * 0 or more

\S Not white space + 1 or more

\s White space ? 0 or 1

\W Not word {3} Exactly 3

\d Digit {3,} 3 or more

\D Not digit {3,5} 3, 4 or 5

\b Word boundary ^ Beginning of String

\B Not word boundary \$ End of String

Regex (cont)

^ matches [matches

] characters NOT in bracket] characters in brackets

| Either Or (Group)

ε Empty string containing no characters

^ [. \$ { * (\ +) | ? < >

Metacharacters need to be escaped

Currying

Currying is the process of transforming a function that takes multiple arguments in a tuple as its argument, into a function that takes just a single argument and returns another function which accepts further arguments, one by one, that the original function would receive in the rest of that tuple.

from g :: (a, b) -> c to f :: a -> (b -> c)

f :: a -> (b -> c) is the same as f :: a -> b -> c

g (x, y) = x + y is an uncurried function, has the type g :: Num a => (a, a) -> a

h x y = x + y is a curried addition, has the type h :: Num c => c -> c -> c

curry g can convert it to a curried function

Fold List

foldl takes a binary operation, a starting value, and the list to fold

foldl (-) 0 [3,5,8] => (((0 - 3) - 5) - 8) => -16

foldl and foldr is under the type class **Foldable**

foldl :: Foldable t => (b -> a -> b)

foldr :: Foldable t => (a -> b -> b)

elem' y ys = foldl (\acc x -> if x == y then True else acc) False ys

Notes

head_r repeats n x = (take n x) == returns True if the first n elements of x equals

swap_ends [] = []

swap_ends [y] = [y]

swap_ends x = last x : (reverse (d

Define a function swap_ends that takes a list a elements swapped.

iterate via standard recursion

iterate1 n f

| n <= 0 = id

| otherwise = f . (iterate1 (n-1)

iterate via foldl

iterate2 n f = foldl (.) id [f | i

f1a :: (b, a) -> (a, b)

f1a = \ (x, y) -> (y, x)

f1b :: a -> [a] -> [[a]]

f1b = \x y -> [[x], y]

f1c :: a -> a -> [a] -> [[a]]

f1c = \x y z -> [x : z, y : z]

f1d :: (a -> Bool) -> [a] -> Int

f1d f = length . (filter f)

(:) :: a -> [a] -> [a]

(++) :: [a] -> [a] -> [a]

++ is only used for list concatenation,

whereas : is used for joining element with lists

Num class does not support /, Fractional does

Pattern Matching

(x:xs) head x and tail xs

(x:3:xs) list where 2nd element is 3

myData a _ c ignore one of the component

-> b -> t a -> b



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Pattern Matching (cont)

```
data Pattern a = P a | POr (Pattern a) (Pattern a) | PAnd (Pattern a) (Pattern a) deriving Show

match pattern [] = (False, [])
match (P x) (y : ys) = if x == y
  then (True, ys) else (False, y : ys)
match (POr pat1 pat2) xs = case m
  atch pat1 xs of
    (True, leftover) -> (True, leftover)
    (False, _) -> match pat2 xs
match (PAnd pat1 pat2) xs = case
  match pat1 xs of
    (False, _) -> (False, xs)
    (True, leftover) -> case match pat2
  leftover of
    (False, _) -> (False, xs)
    (True, leftover2) -> (True, leftover2)
```

Regex Examples

Natural numbers with no leading zeros except just 0

`0 | [1-9] \d*`

Floating point numbers w/o leading zeros

`(0 | [1-9] \d*.\d* | . \d+)?([eE][+-]?[0-9]+)`

Hex numbers allowing leading zeros

`0x[0-9a-fA-F]*`

Strings with an even #a's or number of b's divisible by 2

`(b*ab*a)*b*((a*ba*ba*b)*a*`

Match regular expressions using backtracking

Match regular expressions using backtracking (cont)

```
> match Rend str = FAIL
match Rany "" = FAIL
match Rany (c : cs) = OK [c] cs
match (Rch ch1) "" = FAIL
match (Rch ch1) (str @ (ch2 : left))
  | ch1 == ch2 = OK [ch1] left
  | otherwise = FAIL
match (Ror exp1 exp2) str =
  case match exp1 str of
    FAIL -> match exp2 str
    result1 @ (OK match1 remain1) ->
      case match exp2 str of
        FAIL -> result1
        result2 @ (OK match2 remain2) -
>
      if length match1 >= length
match2
match (Rand exp1 exp2) str =
  case match exp1 str of
    FAIL -> FAIL
    ok @ (OK match1 remain1) ->
      extend match1 (match exp2
remain1)
match (Ropt exp) str = match (Ror exp
Rnull) str
match (Rstar exp) str =
  case match exp str of
    FAIL -> OK "" str
    OK match1 remain1 ->
      if match1 == "" then OK "" str
      else
        extend match1 (match (Ror
(Rstar exp) Rnull) remain1)
extend match1 (OK match2 remain2) = OK
(match1 ++ match2) remain2
extend match1 FAIL = FAIL
-- mkAnd string = the exp that matches
each character of the string in sequence.
--
mkAnd (c : "") = Rch c
mkAnd (c : cs) = Rand (Rch c) (mkAnd cs)
```

Match regular expressions using backtracking (cont)

```
> --
mkOr (c : "") = Rch c
mkOr (c : cs) = Ror (Rch c) (mkOr cs)
```

More Examples

```
(Find out whether a list is a
palindrome)
isPali ndr ome'' :: (Eq a) =>
[a] -> Bool
isPali ndr ome'' xs = foldl
(\acc (a,b) -> if a == b then
acc else False) True input where
input = zip xs (reverse xs)
(Eliminate consec utive
duplicates of list elements)
compress :: Eq a => [a] -> [a]
compress = map head . group
(Count the leaves of a binary
tree)
countL eaves Empty = 0
countL eaves (Branch _ Empty
Empty) = 1
countL eaves (Branch _ left
right) = countL eaves left +
countL eaves right
(User- Defined Polymo rphic
Lists)
(a) Define the function foldList
which acts on user-d efined
lists just as foldr acts on
native lists.
foldList :: (a -> b -> b) -> b -
> List a -> b
foldList f init Nil = init
foldList f init (Cons x xs) = f
x (foldList f init xs)
(b) Define the function sumList
which adds up the entries in an
argument of type (List Int).
sumList :: (List Int) -> Int
sumList = foldList (+) 0
```

```

data RegExp = Rnull
              | Rend
              | Rany
              | Rch
Char
              | Ror
RegExp RegExp
              | Rand
RegExp RegExp
              | Ropt
RegExp
              | Rstar
RegExp
              der -
iving (Eq, Show)
data Mresult = FAIL | OK String
String deriving (Eq, Show)
match :: RegExp -> String ->
Mresult
match Rnull str = OK " " str
match Rend " " = OK " " " "

```

```

data ParseT = STR String | LIST
[ParseT] deriving (Show, Eq,
Read)
data PResult = FAIL | OK
[ParseT] String deriving (Show,
Eq, Read)
type Parser = String -> PResult

```



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Lecture 11 (cont)

```
> type TreeBuilder = [ParseT] -> ParseT --
LIST, for these trees
-- Note use of &> as AND and |> as OR
list = parse LIST (skip "(" &> list &> sublist
&> skip ")")
    |> skip "[" &> list &> sublist &>
skip "]"
    |> identifier)
sublist = (skip ",") &> list &> sublist |> empty
identifier = literal "x"
empty = OK [] -- empty string parser always
succeeds
-- expr = expr &> literal "+" &> identifier |>
empty
-----
-- UTILITY ROUTINES
-- Parse a string and make it a parse tree
literal :: String -> Parser
literal want input =
    let found = take (length want) input
        remainder = dropblank (drop (length
want) input)
    in
        if want == found then OK [STR want]
remainder
        else FAIL
-- Parse a string but don't save it as a parse
tree
skip want input =
    case literal want input of
        FAIL -> FAIL
        OK _ remain -> OK [] remain
-- Remove spaces from head of string
dropblank = Data.List.dropWhile Data.C-
har.isSpace
-----
-- Concatenation and alternation operators
on parsers
-- (|>) is an OR/Alternation operator for
parsers.
--
infixr 2 |>
```

Lecture 11 (cont)

```
> (|>) :: Parser -> Parser -> Parser
(p1 |> p2) input =
    case p1 input of
        m1 @ (OK _ _) -> m1 -- if p1
succeeds, just return what it did
        FAIL -> p2 input
-- (&>) is an AND/Concatenation operator
for parsers
--
infixr 3 &>
(&>) :: Parser -> Parser -> Parser
(p1 &> p2) input =
    case p1 input of
        FAIL -> FAIL -- p1 fails? we fail
        OK ptrees1 remain1 ->
            case p2 remain1 of -- run p2 on
remaining input
                FAIL -> FAIL -- p2 fails? we fail
                OK ptrees2 remain2 -> -- both
succeeded
                    OK (ptrees1 ++ ptrees2)
remain2
-----
-- Building a parse tree from list of found
parse trees
parse :: TreeBuilder -> Parser -> Parser
parse builder parser input =
    case parser input of
        FAIL -> FAIL
        (OK [] remain) -> OK [] remain
        (OK trees remain) -> OK [builder trees]
remain
```



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